

## 2 Conceptual Database Design

### 2.3 Integrity Constraints

#### 2.3.1 Constraint types

#### 2.3.2 Cardinality constraints

### 2.4 Extended ER Modeling

#### 2.4.1 Inheritance / Generalization

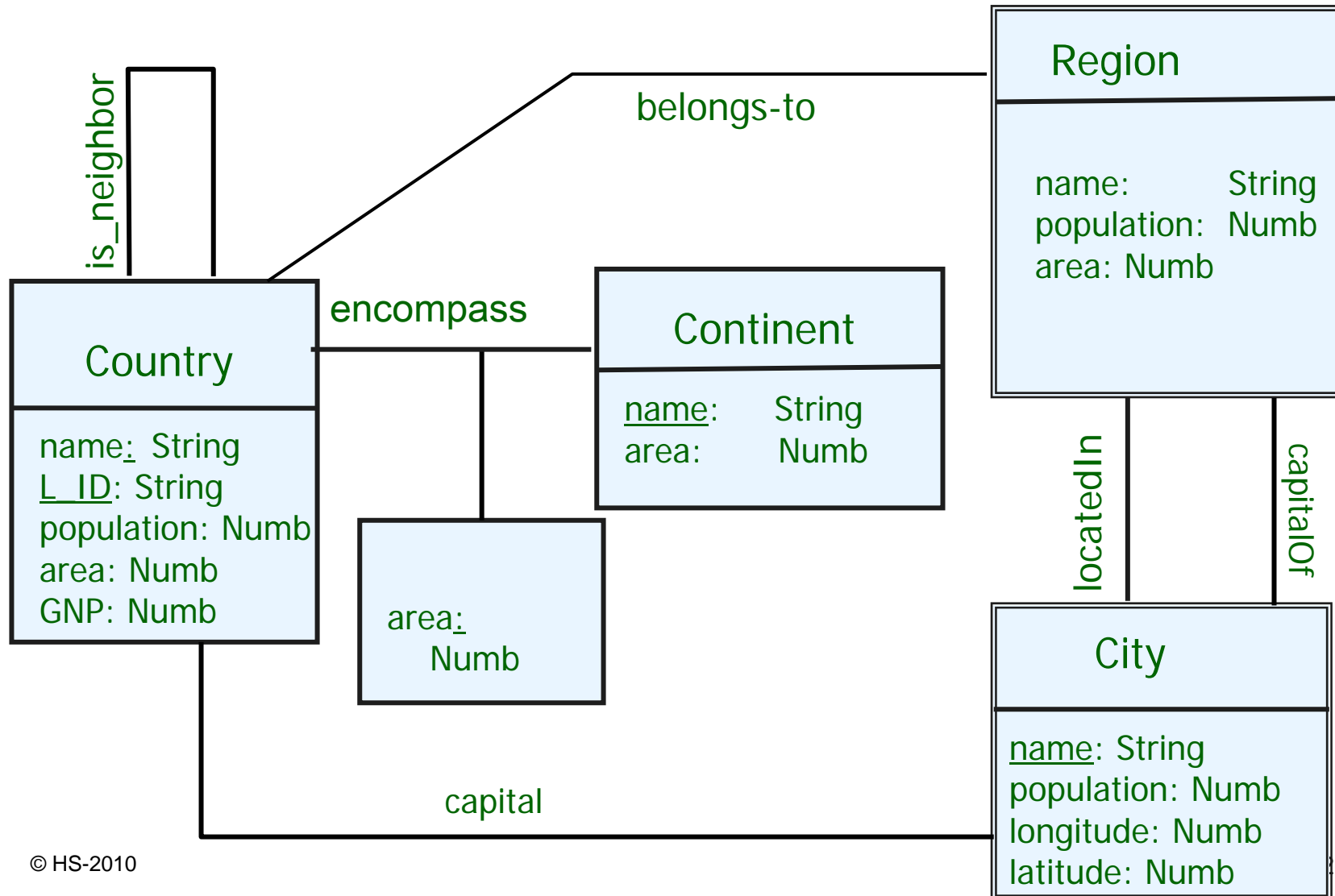
#### 2.4.2 Modeling historical data

#### 2.4.3 N-ary relationships

Bernstein et al.: chap. 4; Elmasri, Navathe: chap 3 + chap 4;  
Kemper, Eickler: 2.7 – 2.13

# Conceptual Design: case study

## Constraints I??



## 2.3.1 Integrity Constraints

Important concept

Def.: An **Integrity constraint** is an invariant (assertion, restriction) of the state of a database.  
ICs are **predicates**, a database must fulfill during its lifetime.

They **result from requirement analysis**, context and common sense knowledge  
**Formally stated** in DB schema

### Case study

From requirements

"Names of regions are not necessarily unique"

"A regions belongs to exactly one country"

Common sense knowledge

"Population is always  $\geq 0$  - or unknown"

"A country has one and only one capital"

# Constraint types

## Attribute constraints

- Attribute value restriction
- Attribute value must / may exist ( [not] NULL ]

## General constraints

- Relations may be symmetric  
e.g. neighbor-rel of countries

## Cardinality constraints

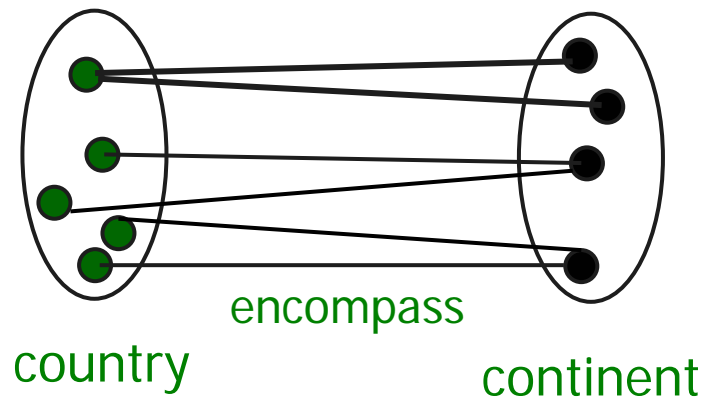
How many entities of type E may be in relationship R to an entity of type E'?

e.g. to how many countries can a region belong?  
How many regions can a country have?

## 2.3.2 Cardinality constraints

Important concept

**Def.:** A **cardinality constraint** of a relationship R between entity types E1', E2' **restricts the number of entities** E1, E2 participating R

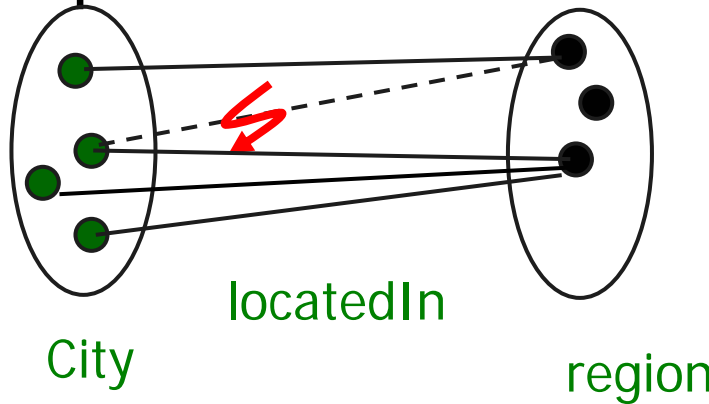


UML terminology: **multiplicity**

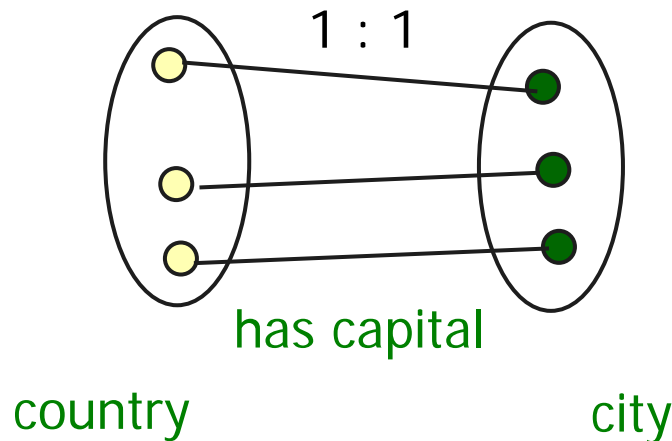
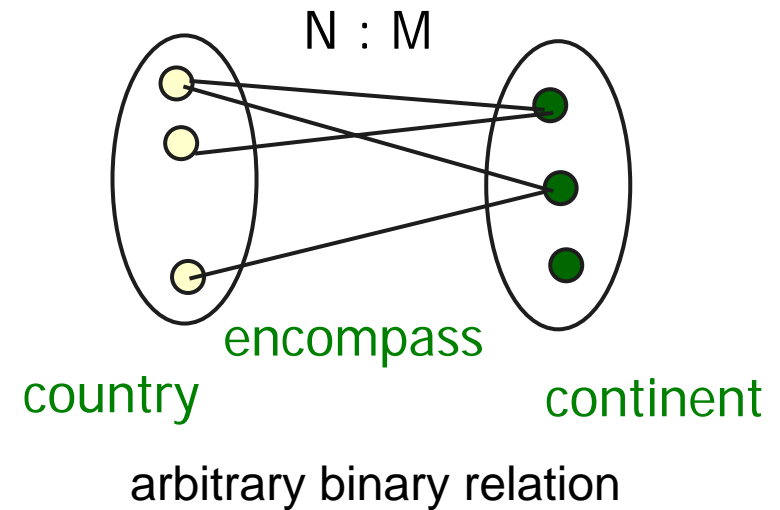
# Cardinality constraints, N:M notation



## Examples



⚡ contradicts 1 : N, not allowed



# 1:N relationship

## Graphical Notation with symbolic cardinalities



One E1-entity is related (R) to arbitrary many E2-entities,  
but one E2-entity is related (R) to only one E1-entity

## Traditional ER-M notation for cardinality constraints

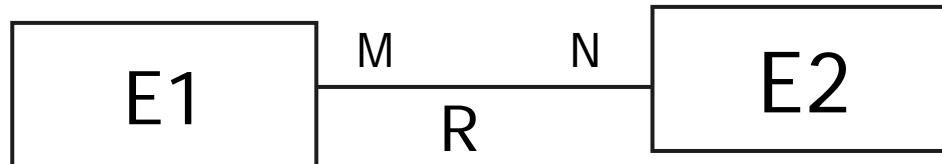


Formally: **locatedIn:: city -> region is a function**

# More relationships

## M:N-Relationships

every instance of E1 may be related according to R to every instance of E2



R is M:N means: **no restriction on the pairs of R**

## 1:1-Relationships

every instance of E1 may be related according to R to exactly one instance of E2 and vice versa





## (min,max)-Notation

More **precise cardinality** restrictions by specifying **minimal and maximal number of entities**

Many cities *located in* one country, at least one

⇒ min=1, max = \*

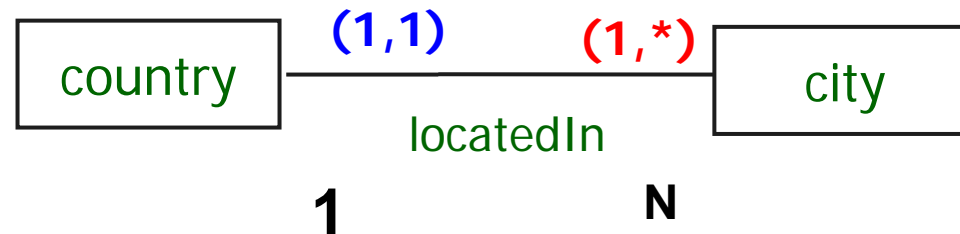
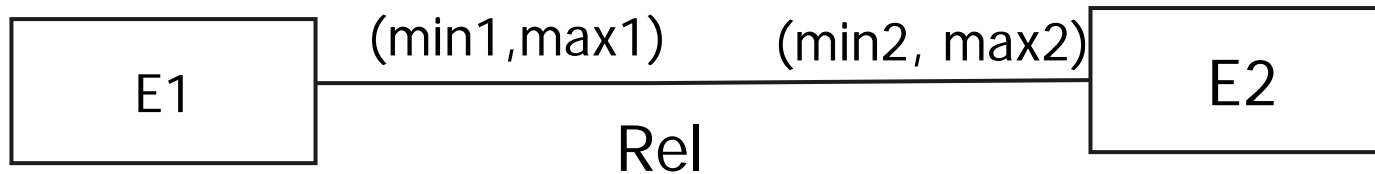
A country has zero, one or many *neighbors*

⇒ min=0, max = \*

**(min,max)-Cardinality constraint (multiplicity) notation**  
also used in **UML associations**.

# (min,max)-Notation

## Graphical notation

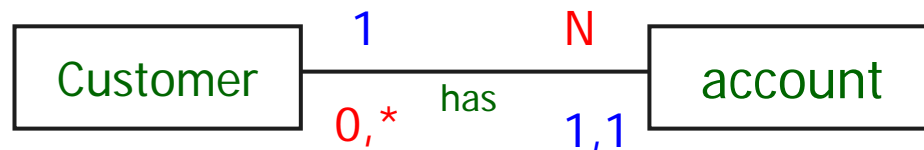


### Note

- **1:N** notation characterizes **relationship R**.
- $(\min, \max)$  characterizes entity and relationship R, in general different for E1 and E2

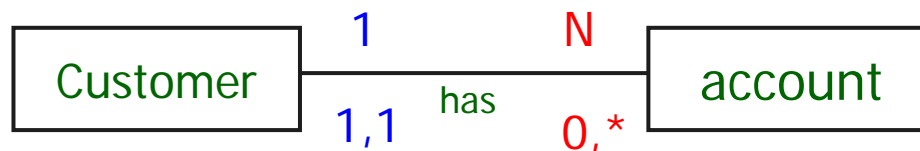
# CAVEAT: Misleading Notation

Traditional ER-Model, (min,max)-Notation **does not conform to N:M-Notation**



You find this in many text books, 1:N and (min,max) interchanged

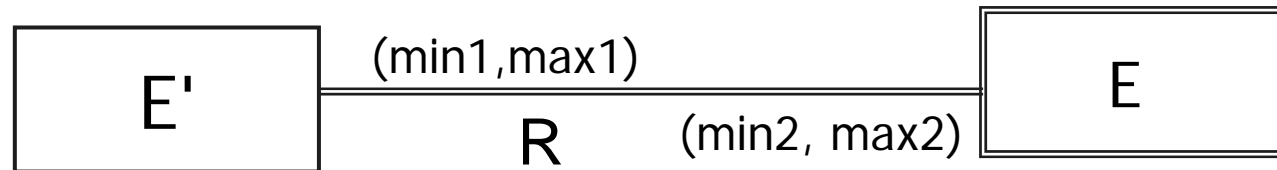
UML-multiplicity conformant to 1:N notation



WE USE THIS NOTATION

Use (min,max) annotation which conforms to UML,  $\text{min,max} \in \{0,1,*\}$

# Cardinality of weak entities



**e is existentially dependent on e'**

**Cardinality:**

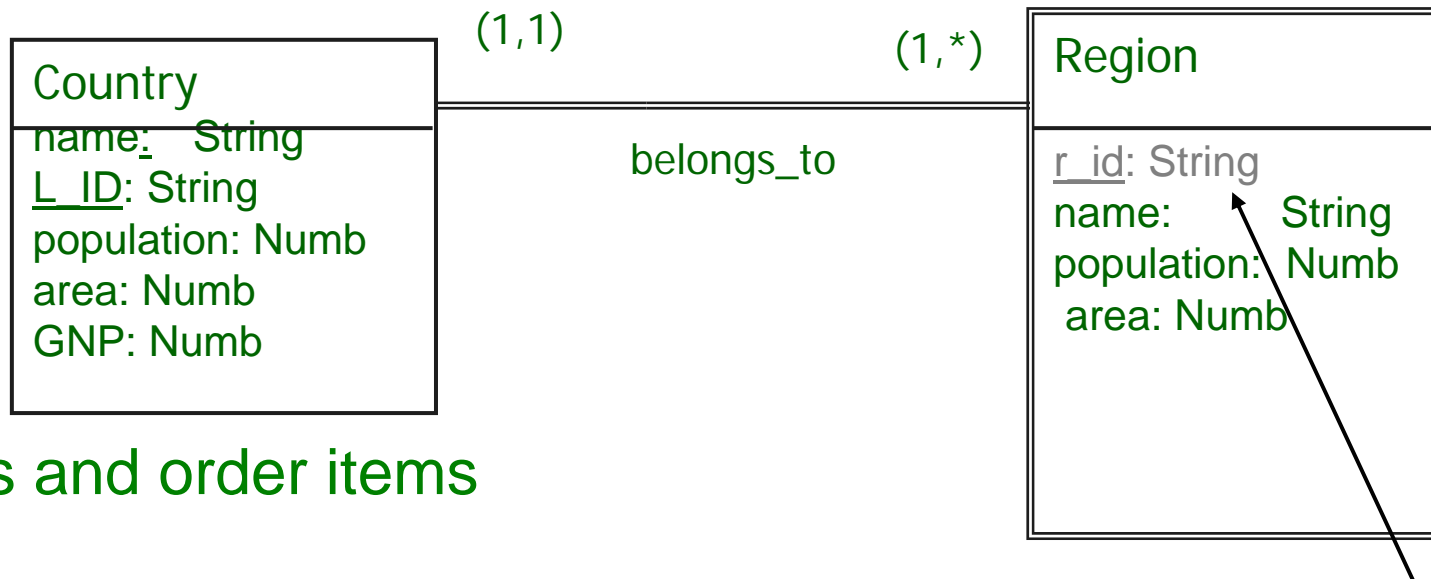
$$\text{min1} = \text{max1} = 1$$

$$\text{min2} = 0 \mid 1$$

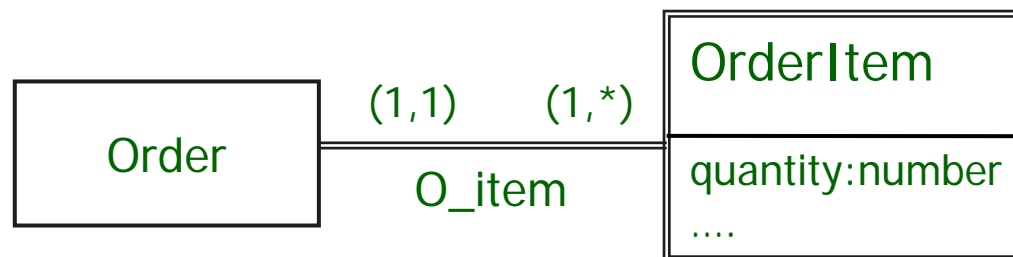
$$\text{max2} = 1 \mid *$$

# Weak entity: example

## Countries and regions



## Orders and order items



Sometimes an artificial key makes sense, not in this case

# Cardinality constraints: semantics

Let  $R \subseteq E1 \times E2$  be a relationship between entity sets  $E1$  and  $E2$

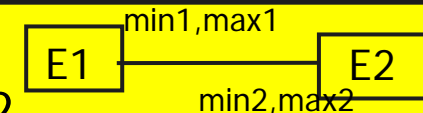
$R$  is 1:N  $\Leftrightarrow R$  is a function  $R: E2 \rightarrow E1$   
 $\Leftrightarrow$  for all extensions of  $R \forall e2 \in E2$ :  
 $|\{e1 \mid e1 \in E1 \wedge (e1, e2) \in R\}| \leq 1$



$R$  is 1:1  $\Leftrightarrow E2 \rightarrow E1$  is an injective function  
 $R$  is M:N  $\Leftrightarrow R$  is a relation, but not a function

Traditional  
ER-M notation!

$E1$ - $R$  has  $(\min1, \max1)$  cardinality  
 $\Leftrightarrow$  for all extensions of  $R$  and for all  $y_0 \in E2$   
 $\min1 \leq |\{x \mid x \in E1 \wedge (x, y_0) \in R\}| \leq \max1$



$E2$ - $R$  has  $(\min2, \max2)$   
 $\Leftrightarrow$  for all extensions of  $R$  and for all  $x_0 \in E1$   
 $\min2 \leq |\{y \mid y \in E2 \wedge (x_0, y) \in R\}| \leq \max2$

# Cardinality constraints notations

	mandatory/ multiple	optional/ multiple	optional/ single	mandatory/ single
ERM / (UML)	(1,*) (1,n)	(0,*) (0,n)	(0,1)	(1,1)
1:N	N or M	N or M	1	1
UML <sup>+</sup>	1 ..* k..j k	0 ..* * 0 .. k	0..1	1

+ : k and j are natural numbers; n, N,M in the ERM are literals

Many more notations in use!, eg. Oracle 'crow's feet'-Notation

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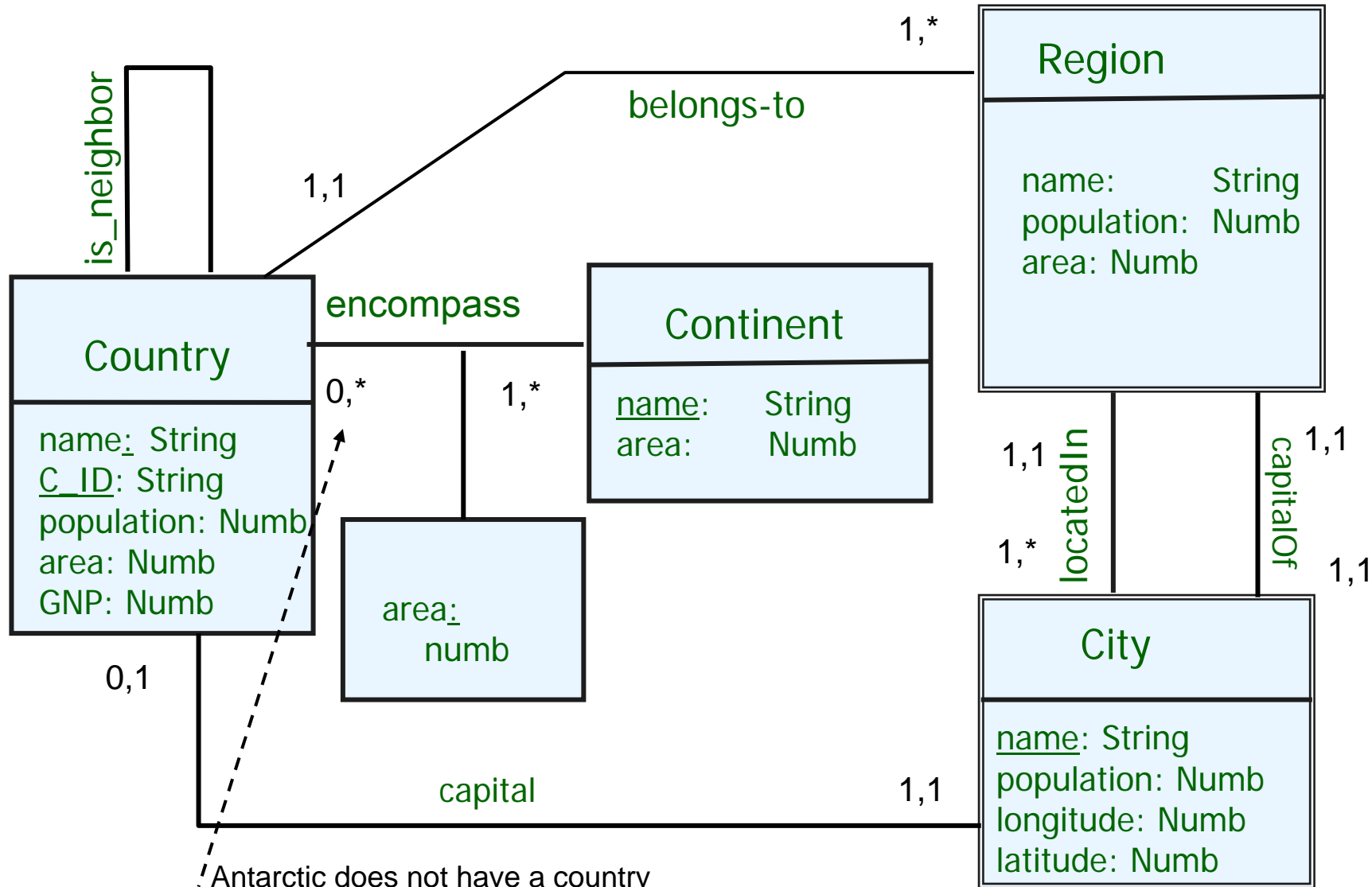
#### 2.4.2 Modeling historical data

#### 2.4.3 N-ary relationships

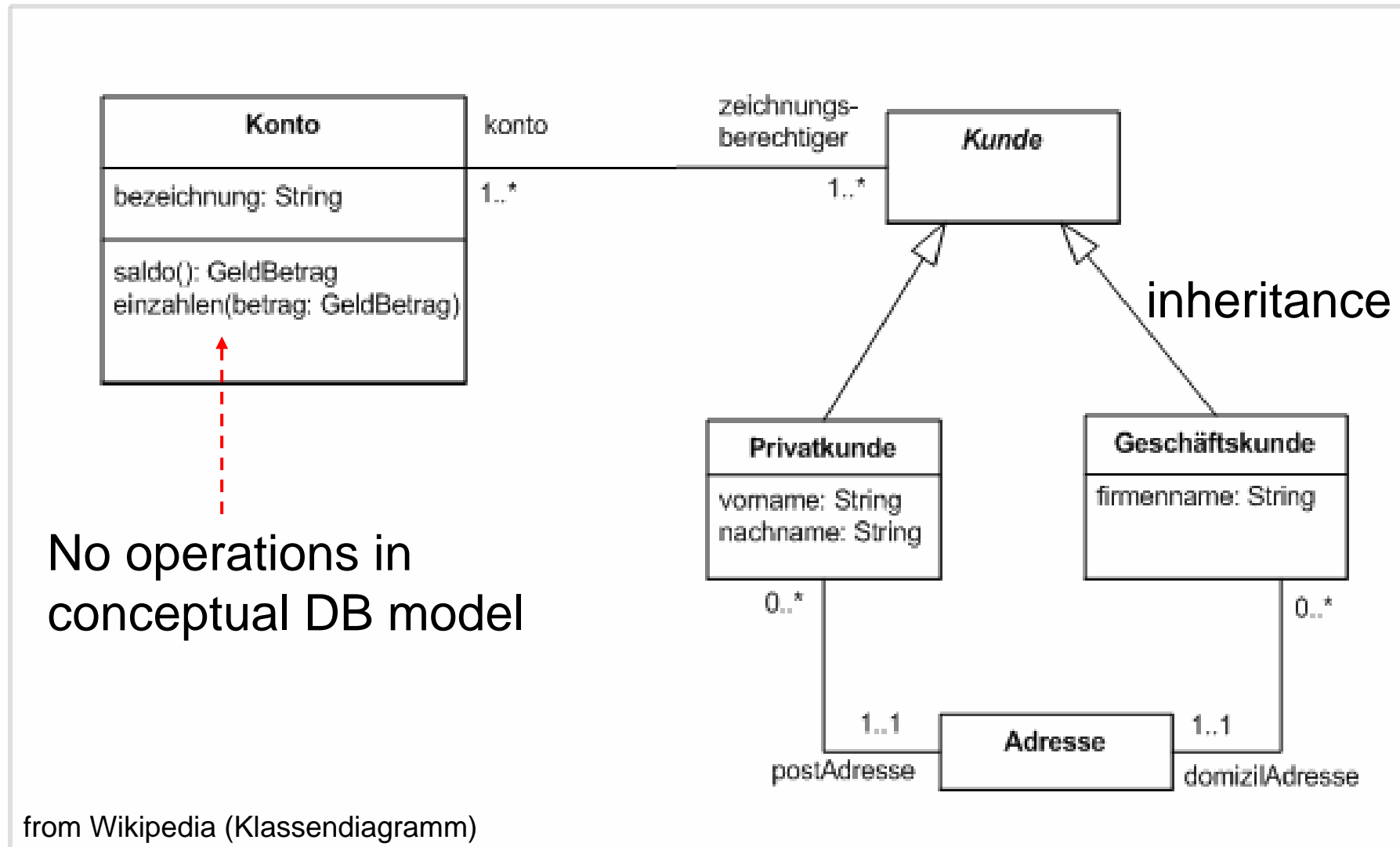
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# Conceptual Design: case study



# UML class diagram



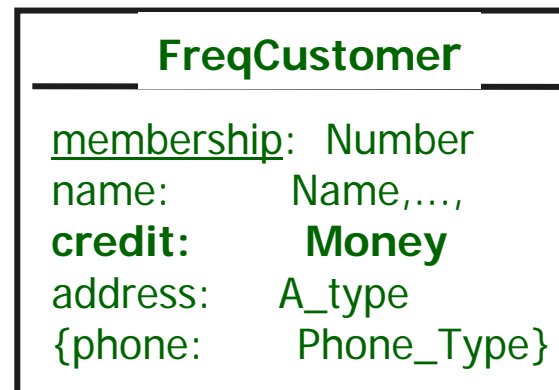
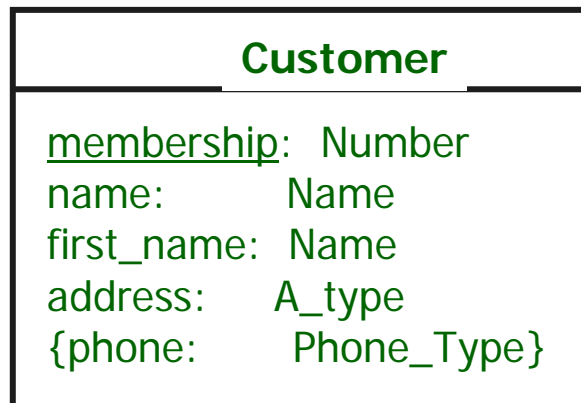
## 2.4 Extended ER (EER)

Example:

Suppose two types of customers of a video-shop:

- frequent customers
- regular customers

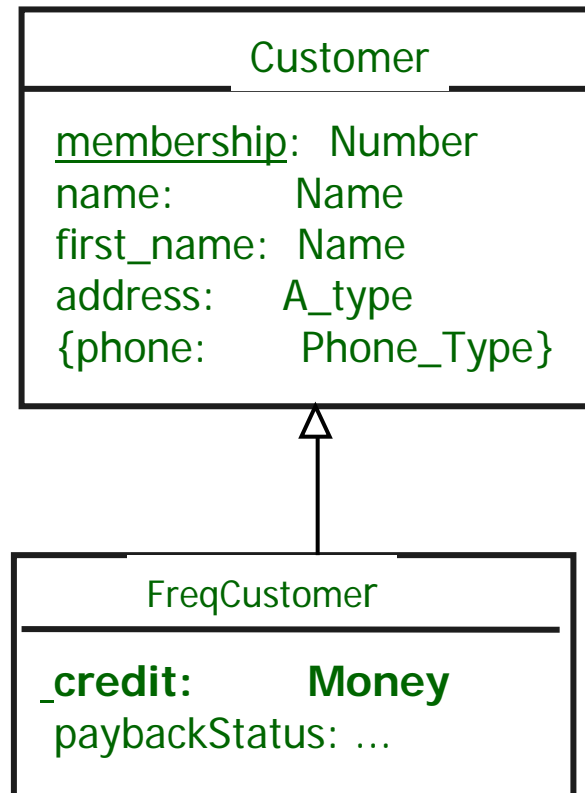
Generalization



*Redundant:*

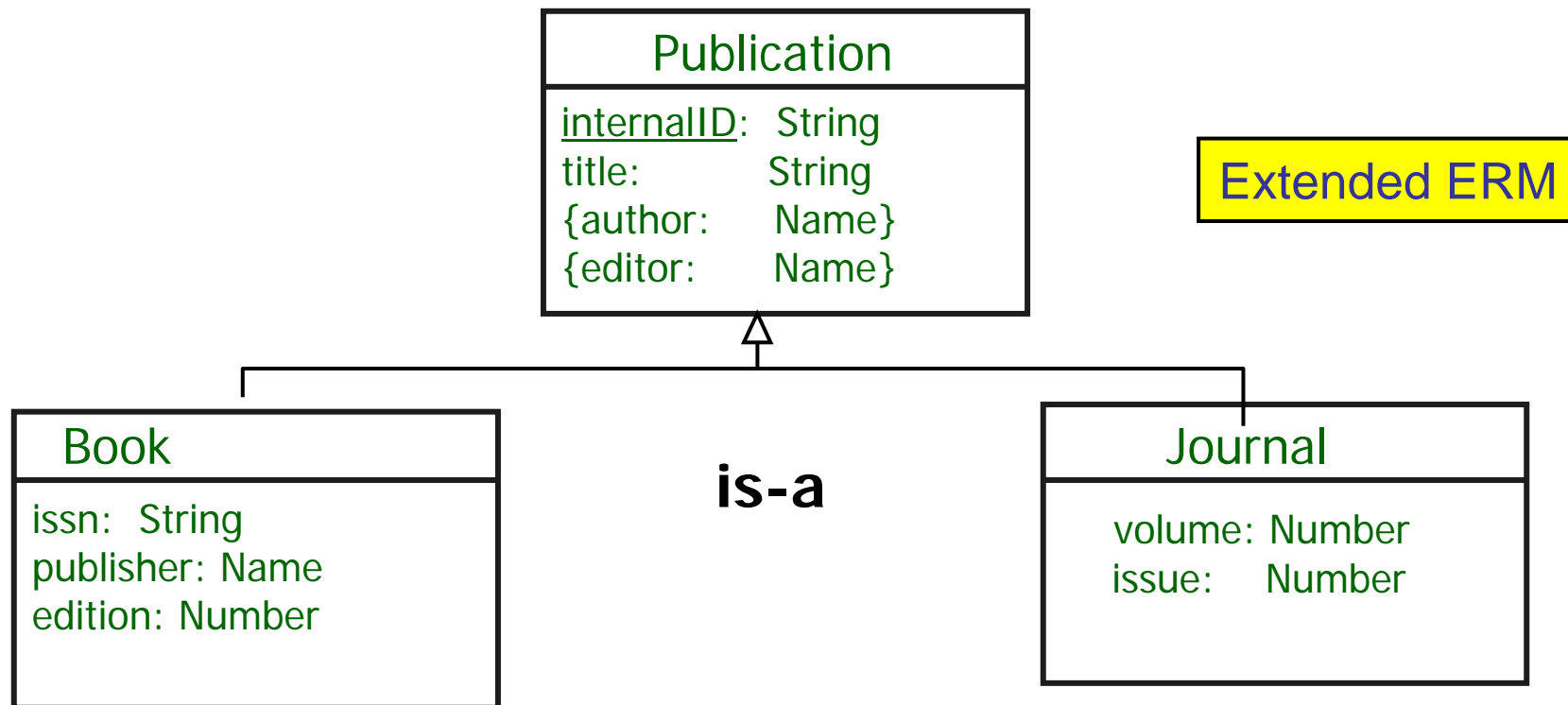
relationships of Customer has to be duplicated for FreqCustomer  
⇒ employ object oriented principle of generalization/ inheritance

# Generalization: Example



## 2.4.1 Generalization / specialization

Factorize common attributes of different entities



Standard relationship **is-a** between subtypes and super types

# Generalization / Spezialisierung

## Semantics of generalization: type versus set

Instances of A, B and C are different but share some attributes (OO-interpretation)

All instances of B and of C are also instances of A (DB interpretation)

$$B \subseteq A \text{ and } C \subseteq A$$

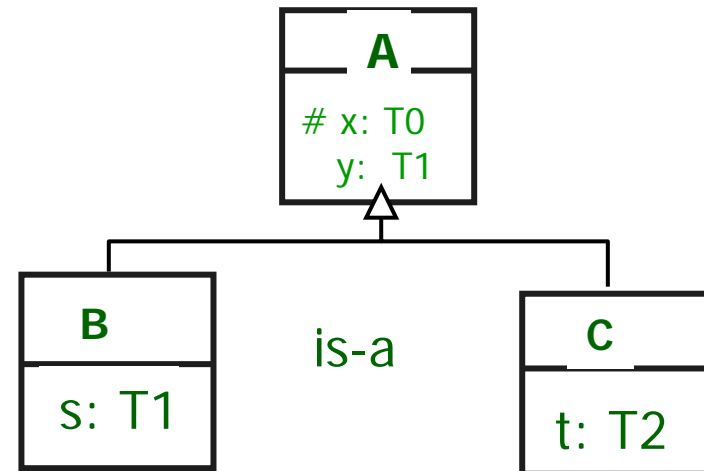
Def.: **Specialization** is called

- **disjoint** iff  $C \cap B = \emptyset$

- **complete**

iff  $A = B \cup C$ ,  
and every tuple is  
either B or C

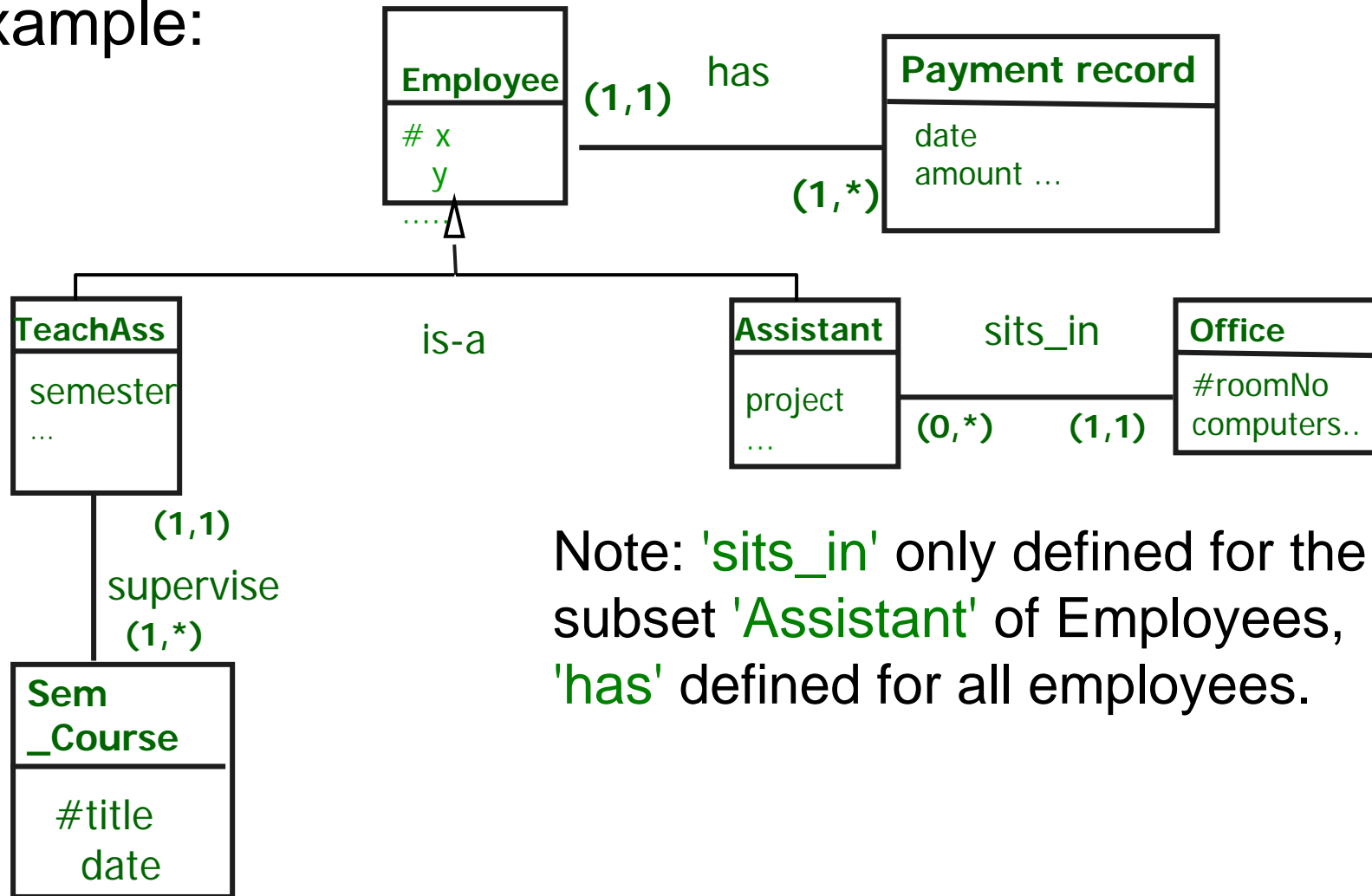
more general definition:  $n > 2$  specializations



No overwriting...  
why not?

# Generalization

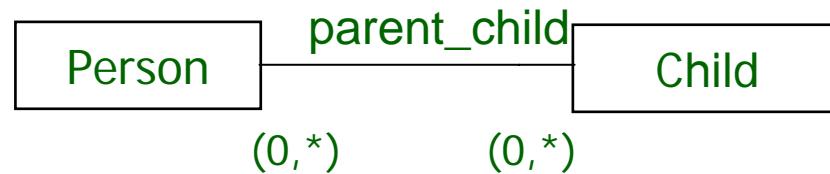
Example:



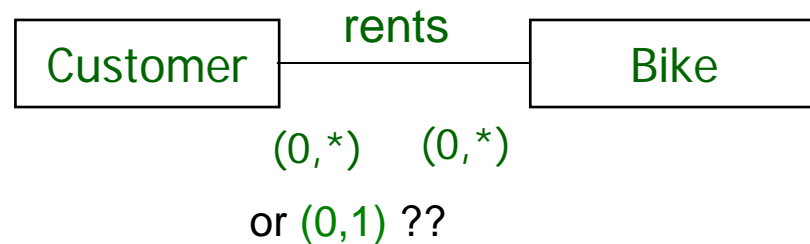
Note: 'sits\_in' only defined for the subset 'Assistant' of Employees, 'has' defined for all employees.

## 2.4.1 Modeling historical data

Important



Time invariant:  
a particular relationship  
between e1 and e2 will  
never change.



Time variant:  
A particular relationship  
(c1, v1) may disappear,  
a new one may be  
established

In many cases:

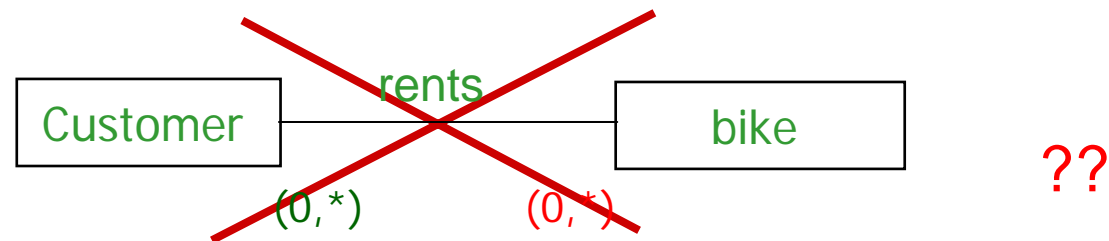
**History of time variant relationships** has to be recorded



# Case study and historical data

Keeping track of changes...

Use case: Bike rental



A bike may be rented by many customers...

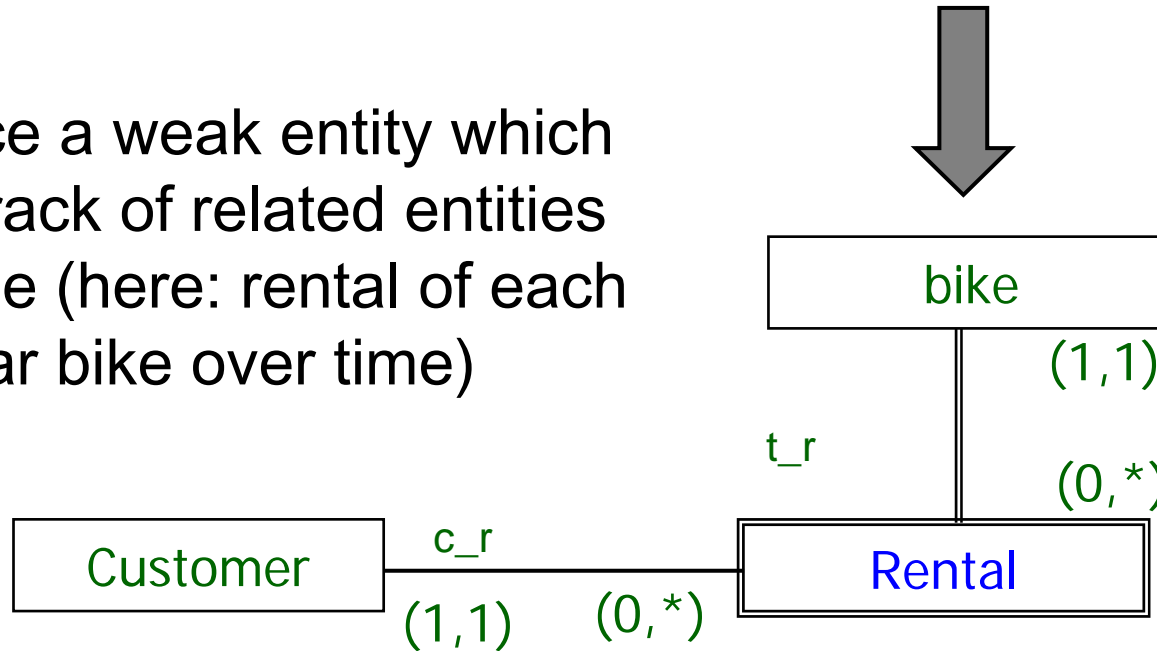
... but not at the same time

# Conceptual Modeling: historical data

Solution:



Introduce a weak entity which keeps track of related entities over time (here: rental of each particular bike over time)

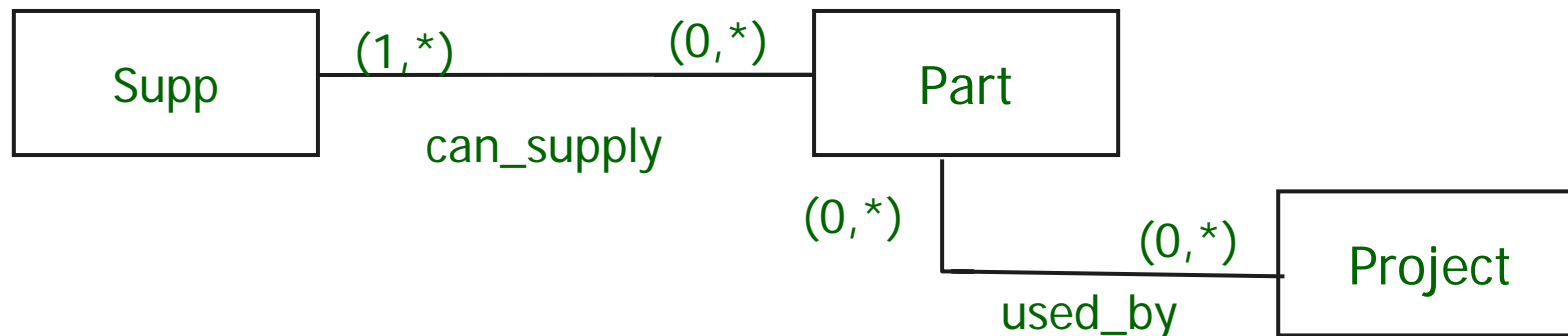


Question: Why 'Rental' existentially dependent on bike, not customer?

## 2.4.2 N-ary relationships

### Motivation example

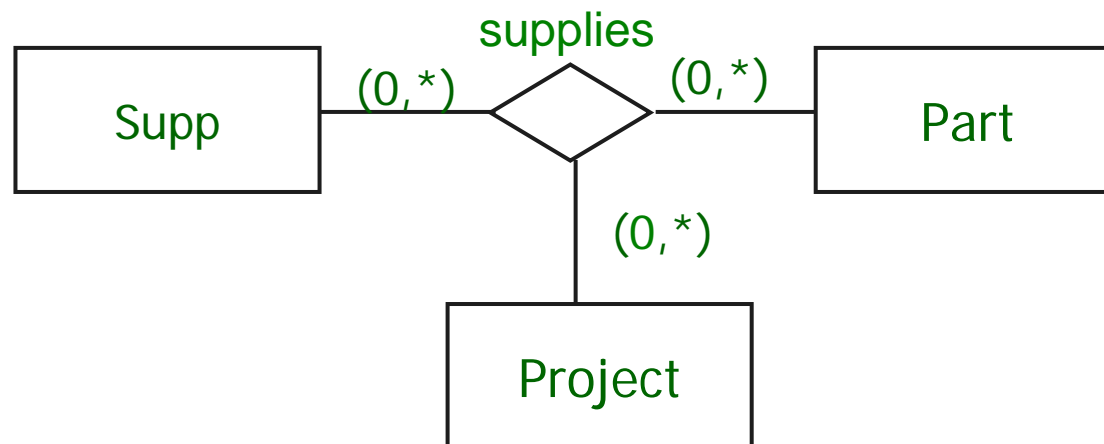
Represent the following facts in a database:  
supplier X delivers part Y to project Z  
supplier A delivers part P to project Z  
supplier B delivers part Q to project S



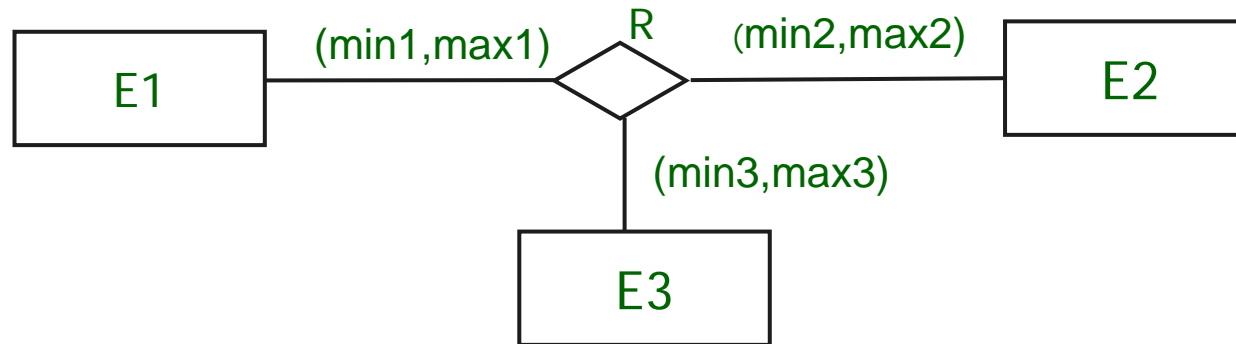
Wrong: Conceptual model does NOT represent the information given above

# N-ary relationships

Def.: A relationship is call **n-ary relationship R**, if more than 2 entity sets are involved in the R



# N-ary relations and cardinalities



Def.:  $E1$ - $R$  has  $(\min1, \max1)$  cardinality

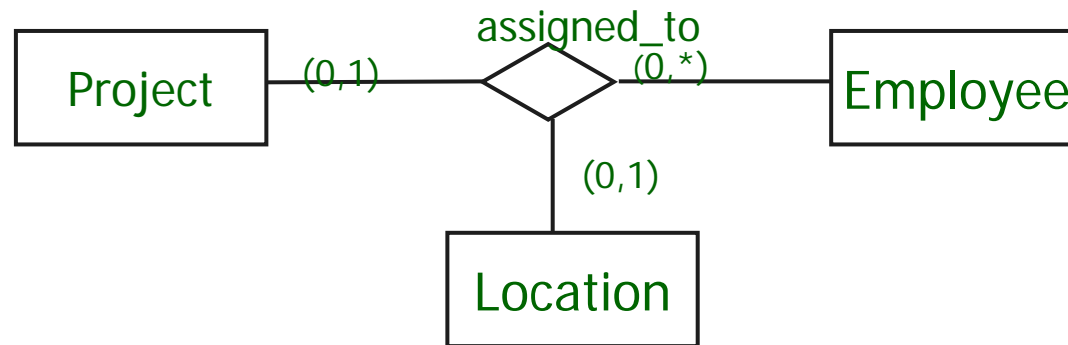
$\Leftrightarrow$  for all extensions of  $R$  and for all  $(y,z) \in E2 \times E3$   
 $\min1 \leq |\{x \mid x \in E1 \wedge (x,y,z) \in R\}| \leq \max1$

$E2$ - $R$ ,  $E3$ - $R$  correspondingly.

# N-ary relationships

Example:

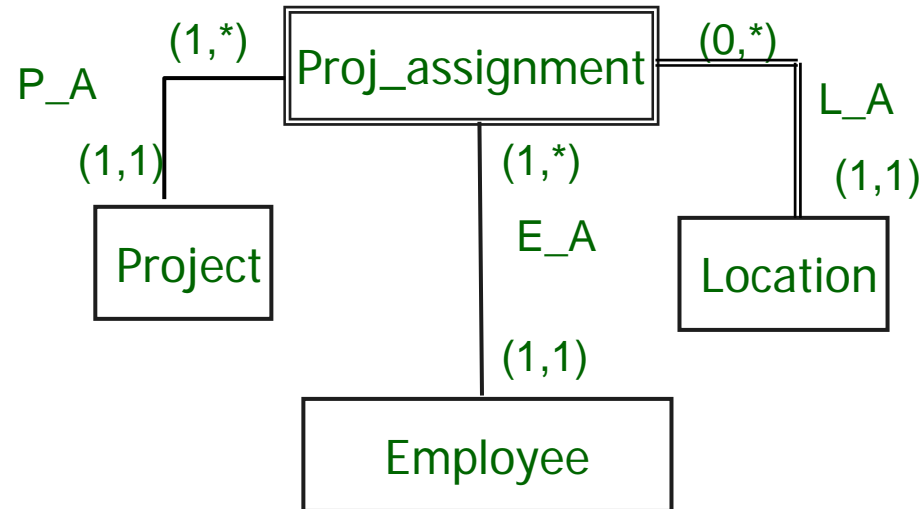
- Employees assigned to a project, work at one location for this project.
- Employees work for one project at a particular location
- At each location several employees may work for a particular project



Question: May an employee work for different projects?

Which constraints cannot be expressed?

# N-ary relationships by N binary relationships

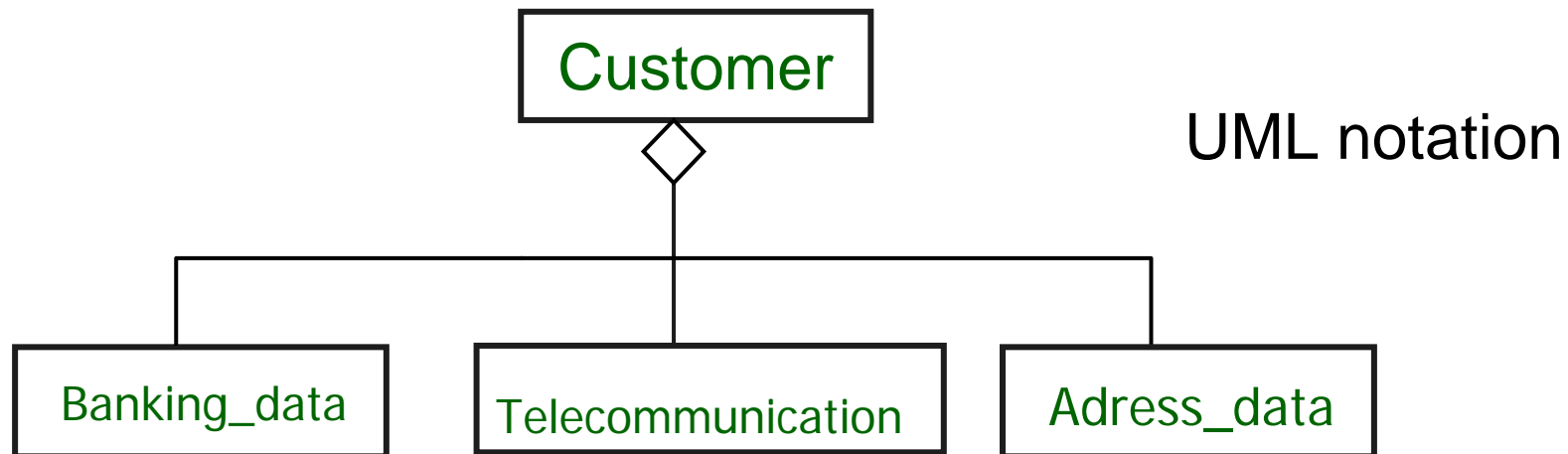


Introduce a **weak entity** type for the relationship and binary relationships to the other entity types.

*Different constraints expressed than n-ary relationship*

# Extended ER: Aggregation

**Aggregate:** different entity types form a new one



Not frequently used in database design

No particular notation for **composition** as in UML



Def.: **View integration** is the process of integrating conceptual models, which are related but have been designed separately, into one single model.

For big projects different "views" of the application make sense: model different, more or less independent parts of the "real world".  
(compare "partitioning approach" to "top down approach")

Important: model **data and processes** the data are used for

e.g. student administration, exams, teachers and human resources

# View integration

Integrate different partial designs into the conceptual design of the overall DB

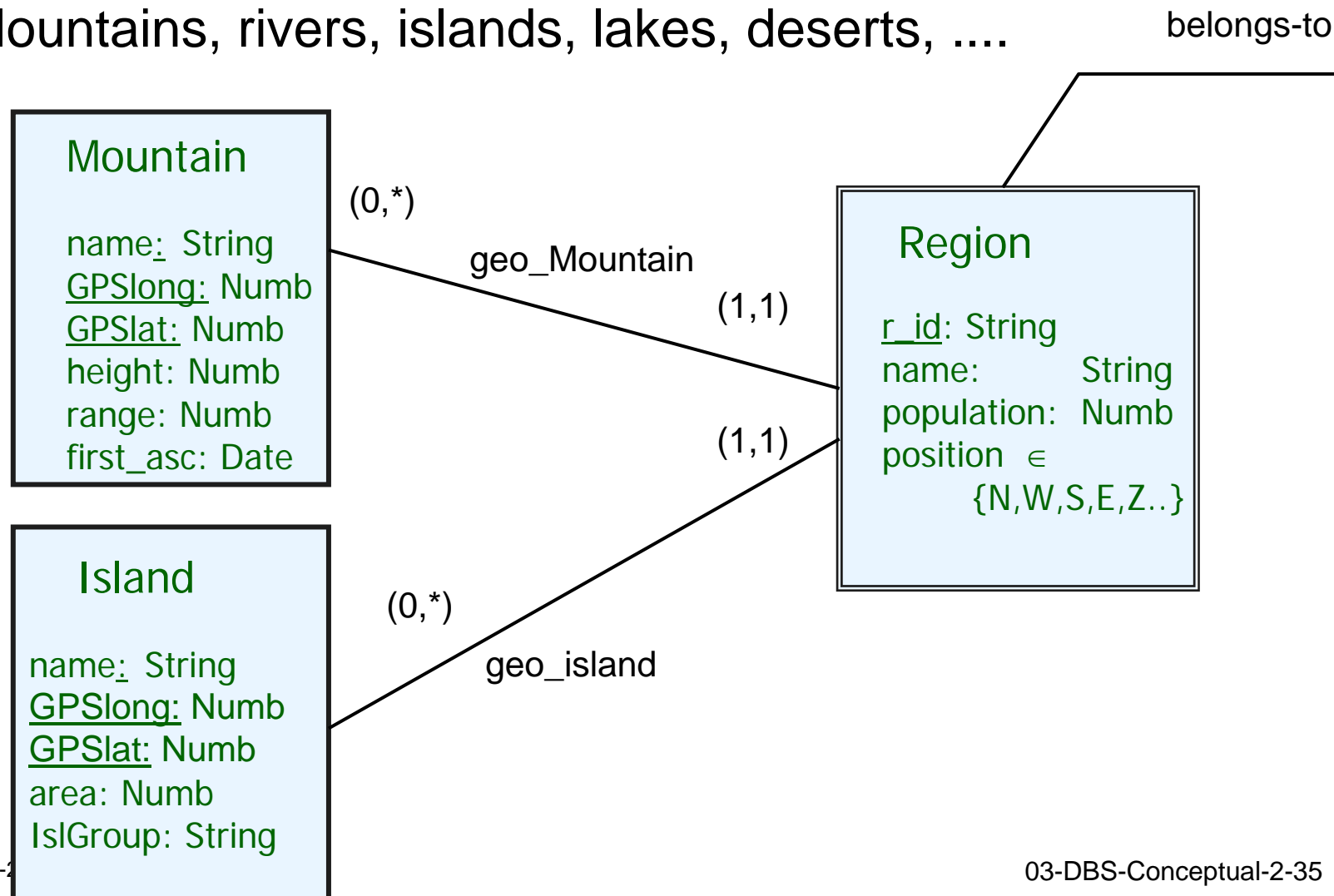
Running example:

- a) countries, cities...
- b) Organizations (Government,  
national / internat. organization
- c) geography: lakes, mountains, rivers...

*Not as easy as it sounds....*

## View integration: "Geography"

Mountains, rivers, islands, lakes, deserts, ....



## Constraints

Restrict the **state** of the database

Database should always be coherent with real world

Types of constraints

- **Value restriction**
- **Cardinality restriction**

1:N notation imprecise but sufficient in many situations

## Uniform modeling "patterns"

Historical / time related data

N-ary relationships: model with binary relationships and a  
another entity type

Generalization