

## 2 Conceptual Database Design

### 2.3 Integrity Constraints

2.3.1 Constraint types

2.3.2 Cardinality constraints

2.3.3 Weak entities

### 2.4 Modeling patterns

2.4.1 Modeling historical data

2.4.2 N-ary relationships

2.4.3 Generalization / specialization ...  
... and more

Elmasri, Navathe: chap 3 + chap 4; Kemper, Eickler: 2.7 – 2.13

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#### • Context

Requirements analysis

Conceptual Design

Schema design  
- logical ("create tables")

Schema design  
- physical  
("create access path")

Loading, administration,  
tuning, maintenance,  
reorganization

System analyst  
DB designer  
Application programmer

Application programmer  
DB administrator

DB administrator

## 2.3.1 Constraint types

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Important  
concept

- Integrity constraints  
(Invariants, assertions, restrictions)
  - A set of predicates, the database must *always* fulfill during its lifetime
  - Taken from requirements, formally stated in DB schema
- Case study
  - "There is always at least one tape for each movie we track, and each tape is always a copy of a single, specific movie"
  - "Not all of our movies have star actors" (Negative constraint)
- Implicit assertions: context knowledge
  - A tape cannot be loaned by more than one customer at a time
  - An actor may be starring in more than one movie

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## Constraint types

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Assertions: constraints which must hold for each state of the database

Similar: Object constraint language (OCL) for UML

- Types of constraints:
  - Attribute constraints
    - Movies are made after 1.1.1900
  - Cardinality constraints
    - Tape can have been lent by zero or one customer at any time
  - General constraints
    - If there exists only a DVD copy of a film, then no extracharge
    - Can be regarded as business rules

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## Constraint types

### Attribute constraints

- Attribute must / may have a value  
Movie has a title, but director not necessarily known
- Value restriction  
Movies are made after 1900 : `movie.year > 1900`

### Typical ERM constraint

- Attributes must not be structured  
attribute `address` with fields `city` `street` etc. not allowed
  - Attributes must have *at most* one value  
~~Phone number: only one allowed~~
- Use set notation for multivalued attributes:  
`{phone_Number}`

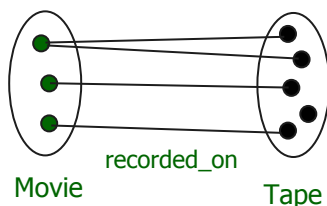
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## 2.3.2 Cardinality constraints

- Restriction of relationships:

Important  
concept

let  $\langle r \rangle$  be a relationship of  $\langle E1 \rangle$  and  $\langle E2 \rangle$   
how many instances of  $\langle E1 \rangle$  may be related  
according to  $\langle r \rangle$  to a single instance of  $\langle E2 \rangle$   
and vice versa?



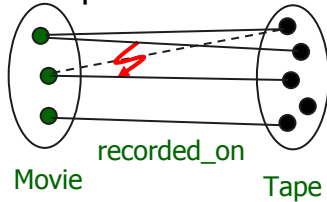
- Number of copies of a movie  $\geq 1$
- A tape can be loaned by at most one customer at a time
- Number of tapes a customer has rented  $\geq 0$
- Exactly one movie on a tape

UML terminology: multiplicity

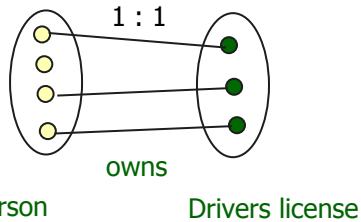
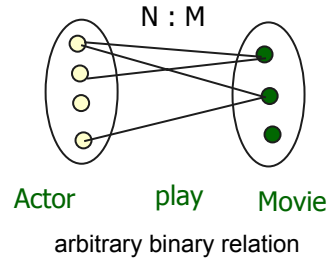
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## Cardinality constraints N:M notation

- Examples



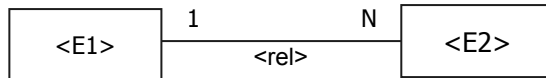
⚡ contradicts 1 : N, not allowed



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## Cardinality constraints N:M notation

- Graphical Notation with symbolic cardinalities



Classical ER-M notation for cardinality constraints



A particular movie may exist (as a copy) on many tapes,  
but a particular tape stores a copy of only one movie.

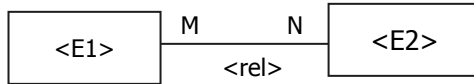
Formally: `recorded_on :: Tape -> Movie` is a function  
Expresses the fact that **the movie on a tape is unique**

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## Cardinality constraints N:M notation

- M:N-Relationships

every instance of <E1> may be related according to <rel> to every instance of <E2>

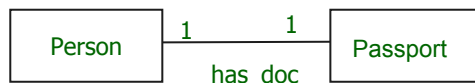
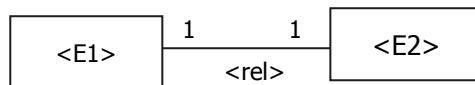


Actors play in one or many movies,  
in a movie typically many actors play.

## Cardinality constraints N:M notation

- 1:1-Relationships

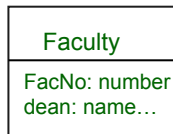
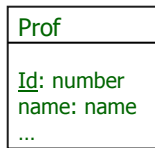
every instance of <E1> may be related according to <rel> to every instance of <E2>



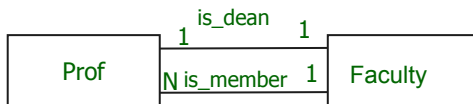
1:1 relationships: not frequently used

## Cardinality constraints and modeling alternatives

- Case: University administration  
among others: faculties and professors  
how to model the *dean* of a faculty?



As an attribute:

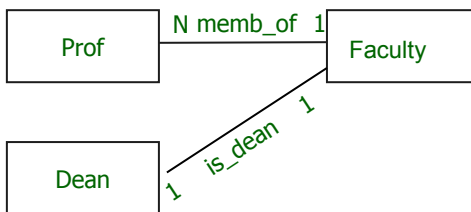


As a relationship:  
Faculty has only one dean, prof may be dean of only one faculty.

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## Cardinality constraints and modeling alternatives (2)

- Case study continued:



Entity:  
Could make sense, if the dean must not be a professor

Note: in both cases "is\_dean" is a 1:1 – relationship

But: every dean *entity* is the dean of one faculty.

As opposed to: every prof is dean *or not*.

Means: Function `is_dean::Fac -> Prof` is not surjective

Difference cannot be expressed until now!

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## Cardinality constraints (min,max)-Notation

### (min,max)–Notation for cardinality constraints

1: N – Notation not strong enough to express all cardinality constraints

#### Minimal values

e.g. zero tapes rented by a particular customer  
or each tape stores a copy of a movie ("at least one")

#### Maximal values

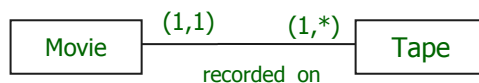
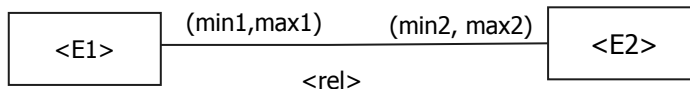
e.g. on a tape there is at most one movie ("at most one")  
a customer may rent arbitrary many tapes ("many")

Cardinality constraint (multiplicity) notation is also used in UML

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## Cardinality constraints (min,max)-Notation

### Graphical notation



"A particular movie may occur 1 or many times in this relation"  
or: "For each movie in the DB there is at least one tape" and  
"There are no empty tapes"

min := 0	1	means: optional	mandatory
max := 1	*	means: single	multiple

Sometimes natural numbers used for min, max  
Does not make much sense, since systems are unable to check  
these fine granular constraints

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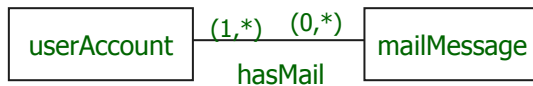
## Cardinality constraints example

- Another example

A database supported email system is designed to have user accounts and mail messages related by the relationship "has mail".

Constraint :

- user has zero or more mails
- mail message belongs to at least one user, perhaps to many users (those with many receivers)

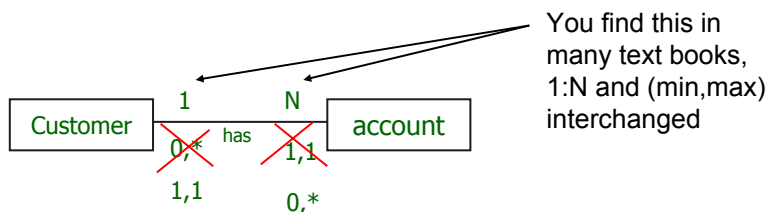


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## Cardinality constraints notations

### Important note

In the classical ER-Model, (min,max)-Notation does **not** conform to the N:M-Notation



Good news:

UML-multiplicity is conformant to 1:N notation.

We use UML-multiplicity with (min,max) annotation,  $\text{min,max} \in \{0, 1, *\}$

laxly : "1:N – relationship", "N:M – relationship" HS / DBS05-concMod-2 16



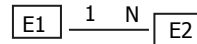
## Cardinality constraints semantics

Let  $R \subseteq E1 \times E2$  be a relationship between entity sets  $E1$  and  $E2$

$R$  is **1:N**  $\Leftrightarrow R$  is a function  $R: E2 \rightarrow E1$

$\Leftrightarrow$  for all extensions of  $R \forall e2 \in E2:$

$|\{e1 \mid e1 \in E1 \wedge (e1, e2) \in R\}| \leq 1$



$R$  is **1:1**  $\Leftrightarrow E2 \rightarrow E1$  is an injective function

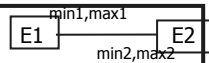
$R$  is **M:N**  $\Leftrightarrow R$  is a relation, but not a function

Classic ER-M notation!

$E1$ - $R$  has **(min1, max1)** cardinality

$\Leftrightarrow$  for all extensions of  $R$  and for all  $y \in E2$

$\min1 \leq |\{x \mid x \in E1 \wedge (x, y) \in R\}| \leq \max1$



$E2$ - $R$  has **(min2, max2)**

$\Leftrightarrow$  for all extensions of  $R$  and for all  $x \in E1$

$\min2 \leq |\{y \mid y \in E2 \wedge (x, y) \in R\}| \leq \max2$

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## Cardinality constraints notations

	mandatory/ multiple	optional/ multiple	optional/ single	mandatory / single
E-RM / (UML)	(1,*) (1,n)	(0,*) (0,n)	(0,1)	(1,1)
E- RM/1:N	N or M	N or M	1	1
UML <sup>+</sup>	1..* k..j k	0..* * 0..k	0..1	1

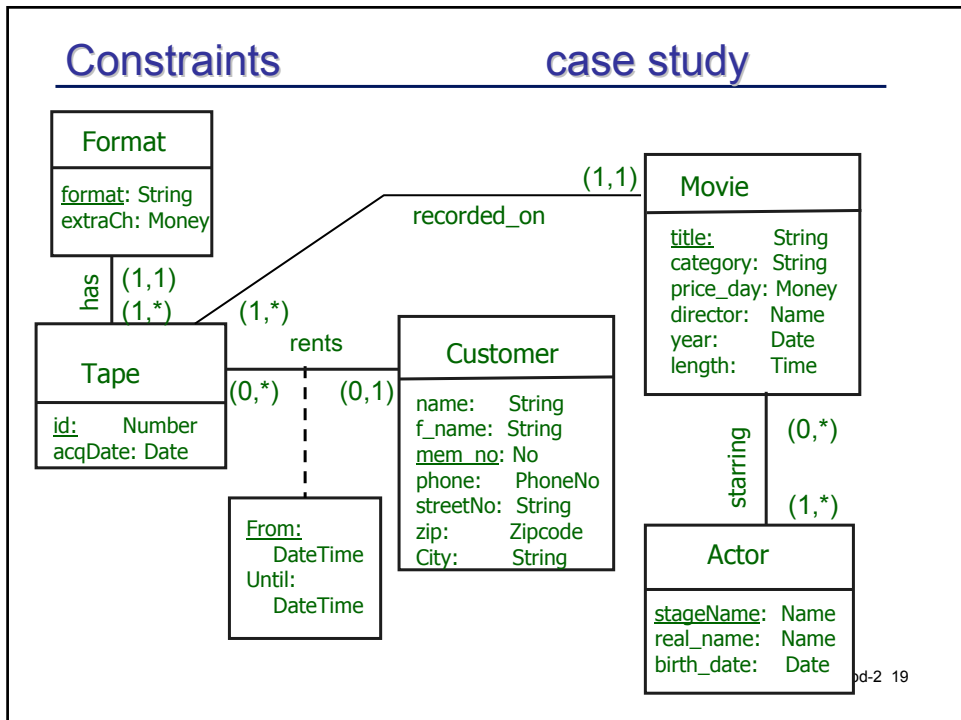
<sup>+</sup> : k and j are natural numbers; n, N, M in the ERM are literals

More notations in use!, eg. Oracle 'crow's feet'-Notation

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## Constraints

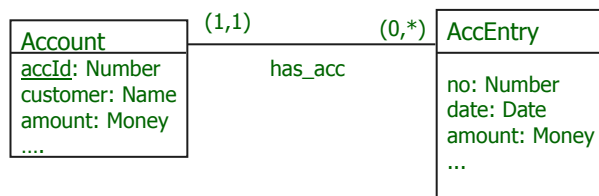
## case study



### 2.3.3 Weak entities

Motivating example:

modeling of bank accounts and the transaction history for each account



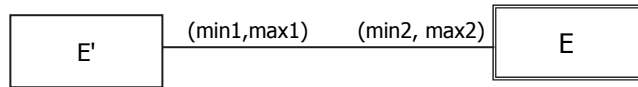
- Issue

one of the entities (accounting entry, **AccEntry**) does not have a key. Uniqueness cannot be guaranteed without referring to a related entity (here: **account**).

"There may be many entries "4711" but only one for a particular account"

## Conceptual Modeling Weak entities

- Weak entity:  
an entity  $e$  of type  $E$ , which is only identifiable by a value  $k$  and the key  $k'$  of one entity  $e'$  of a different type  $E'$ .
- $e$  is said to be **existentially dependent on  $e'$**  (on the entity type level:  $E$  dependent on  $E'$ )
- Notation



- Cardinality:  $\min 1 = 1$   
 $\max 1 = 1$  : why?  
 $\min 2, \max 2$  ?

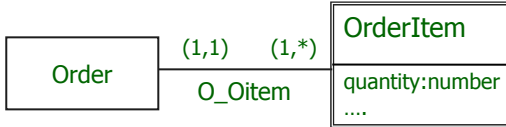
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## Conceptual Modeling Weak entities and UML

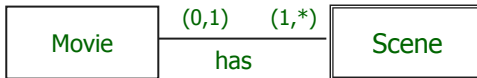
- No weak entities in UML  
each object has identity by its "object id", which is a pointer, referencing the object
- Database modeling paradigm:  
Objects (entities) with identical values for all attributes are identical (like in mathematical sets), except for weak entities
- Object oriented modeling paradigm  
Any two objects are distinguishable by their oid (a physical address!), even if all attributes have the same value

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- More examples

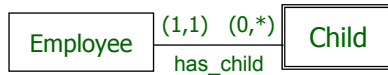


Orders and the items ordered

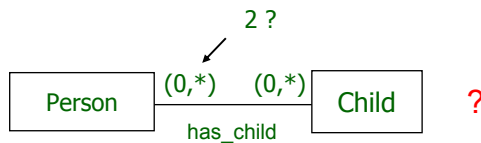


A movie and its scenes

- Modeling decision not always evident



or



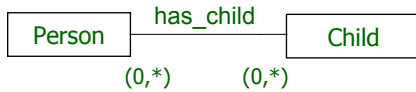
pros and cons?

## 2.4.1 Modeling historical data

- What are historical data?

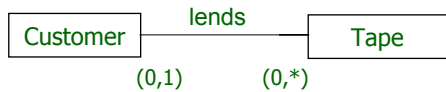
Important

Not time related:



time invariant: a particular relationship between e1 and e2 will never change.  
Rare case.

Time variant



A particular relationship (c1, v1) disappears when tape has been returned

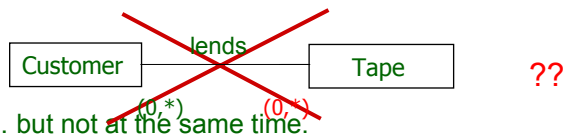
Acceptable but in most cases we want to keep track of the history

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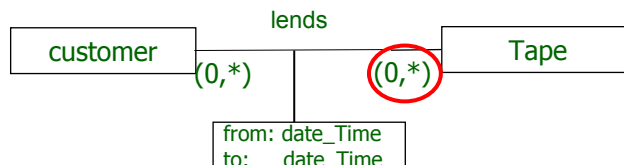
## Historical data

Keeping track of changes...

A tape may be rented by many customers...



Yet another way to model reality...

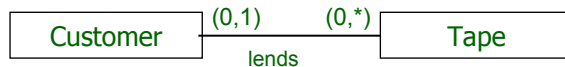


...but constraint lost: a tape is lent to at most one customer

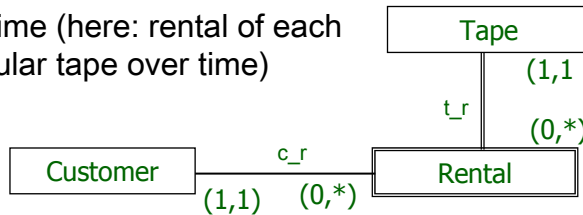
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## Conceptual Modeling: historical data

Solution:

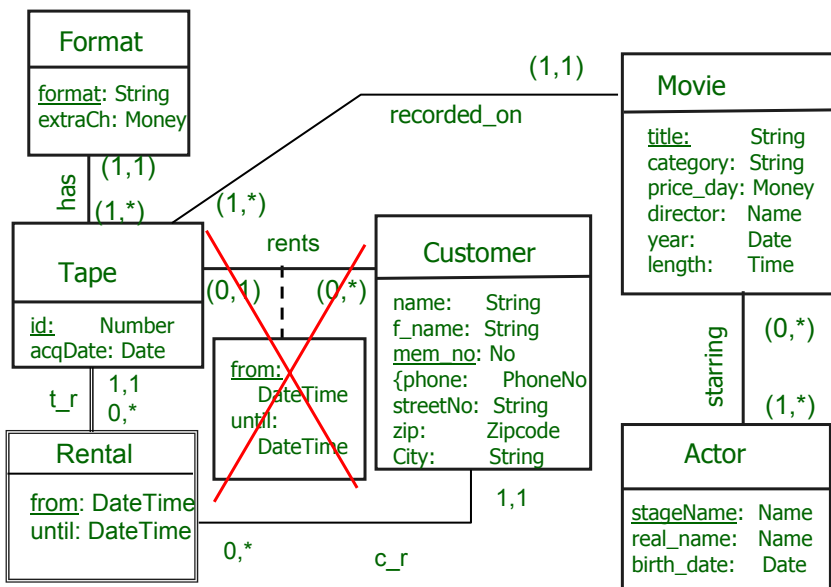


Introduce a weak entity which keeps track of related entities over time (here: rental of each particular tape over time)



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## Case study revised



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## 2.4.2 N-ary relationships

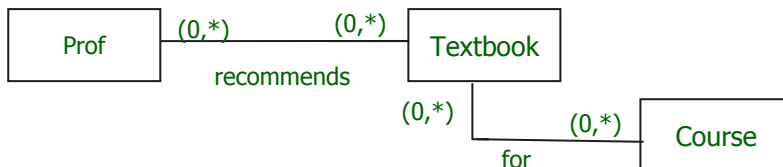
- Motivation example

Suppose you want to represent the following facts in a university database:

prof X suggests textbook Y for course A

prof X suggests textbook T for course B

prof Z suggests textbook T for course A

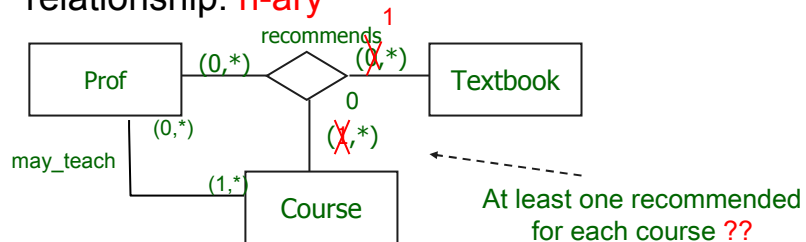


**Wrong:** Conceptual model does NOT represent the information given above

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## N-ary relationships

- More than two entity sets involved in one relationship: **n-ary**



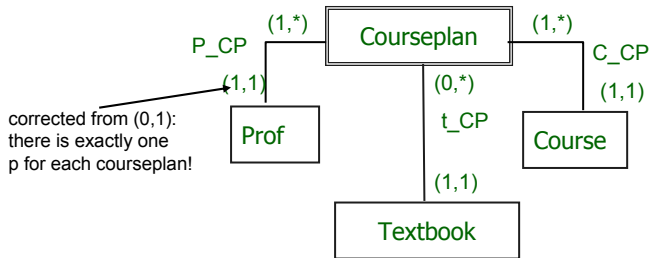
- Cardinality

Each prof is entitled to recommend at least one book for a course -> (1,\*)

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## N-ary relationships modeled binary

- N-ary relationships expressed by binaries



- Introduce a **weak entity** type for the relationship and binary relationships to the other entity types, weak entity may be dependent from any of the other three entity types.

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## 2 Conceptual Database Design

### 2.3 Integrity Constraints

- 2.3.1 Constraint types
- 2.3.2 Cardinality constraints
- 2.3.3 Weak entities

### 2.4 Modeling patterns

- 2.4.1 Modeling historical data
- 2.4.2 N-ary relationships
- 2.4.3 Generalization / specialization ...  
... and more

Elmasri, Navathe: chap 3 + chap 4; Kemper, Eickler: 2.7 – 2.13



## 2.4.3 Generalization / Specialization

- Modeling similar objects by totally different entities is confusing

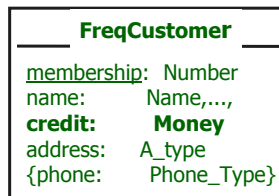
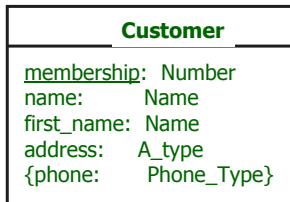
Example:

Suppose two types of customers of the video-shop:

- frequent customers
- regular customers

both have most attributes in common, e.g. membership, address, name

Frequent customers have a "credit line" and some more attributes

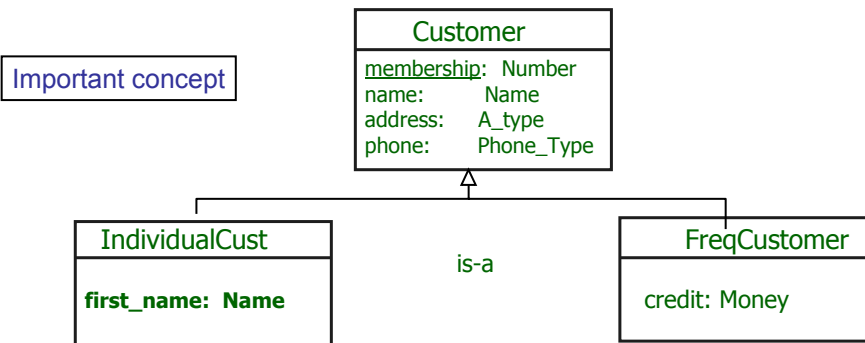


Redundant: employ  
OO principle  
of generalization  
/ inheritance

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## Generalization / specialization

- Generalization / specialization hierarchy allows to factorize common attributes of different entities

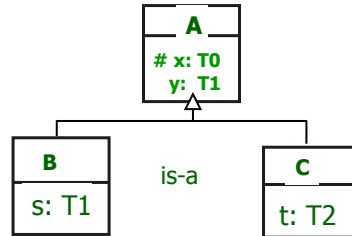


Standard relationship *is-a* between subtypes and super types  
Note: not really types but sets, see next slide

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## Generalization / Spezialisierung

- Different semantics of generalization: type versus set
  - Instances of A, B and C are different (OO-interpretation) but share some attributes
  - All instances of B and of C are also instances of A (DB-interpretation)  
 $B \subseteq A$  and  $C \subseteq A$
  - "is-a" therefore different from ordinary relationships
- Special cases:
  - Disjoint specialization:  $C \cap B = \emptyset$
  - Complete specialization:  $A = B \cup C$ , no extra tuple in A

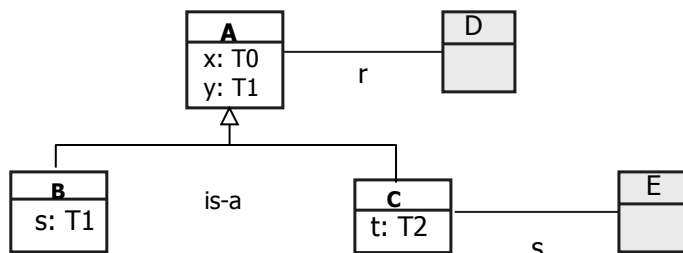


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## Generalization and relationships

- Different relationships may be defined for different entity types of the generalization hierarchy

If A is a generalization of B and C, then all relationships defined for A are implicit relationships for all entities of type B and C

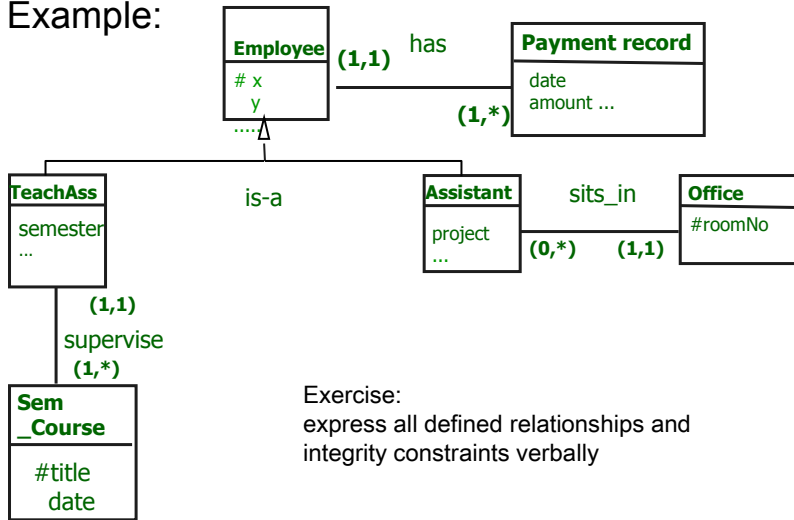


- Entities from entity set A - and therefore those of B and C are related by r to entities from D
- Only entities from set C are related by s to entities from E

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## Generalization

- Example:

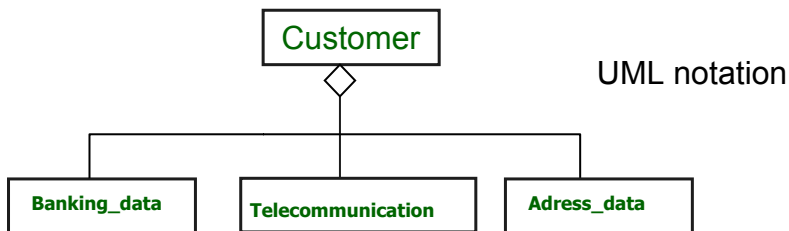


Exercise:  
express all defined relationships and  
integrity constraints verbally

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## Aggregation

Aggregat: different entity types form a new one



Not frequently used in database design

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## Conceptual Design

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### View integration

For big projects different "views" of the application are modeled independently

Very important: model **data and processes** the data are used for

e.g. student administration, exams, teachers and personnel

Integrate different partial designs

→ Conceptual design of the overall DB

Not as easy as it sounds....

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## DB design and constraints

### Short summary

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- **Constraints**

- Restrict the state of the database
- Database should always be coherent with real world
- Types of constraints
  - Value restriction
  - Cardinality restriction
- 1:N notation imprecise, use only for oral communication
- Use (min,max)-Notation coherent with UML

- **Uniform modeling "patterns"**

- Historical / time related data
- N-ary relationships: model with binary relationships and a another entity type
- Generalization

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